

Neutron scattering investigation of rhenium orbital ordering in the 3d-5d double perovskite $\text{Ca}_2\text{FeReO}_6$

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We have carried out inelastic neutron scattering experiments to study magnetic excitations in the ordered double perovskite $\text{Ca}_2\text{FeReO}_6$. We have found a well-defined magnon mode with a bandwidth of ~ 50 meV below the ferrimagnetic ordering temperature ($T_c \sim 520$ K), similar to the previously studied $\text{Ba}_2\text{FeReO}_6$. The spin excitation is gapless for most temperatures within the magnetically ordered phase. However, a spin gap of ~ 10 meV opens up below ~ 150 K, which is well below the magnetic ordering temperature but coincides with a previously reported metal-insulator transition and onset of structural distortion. The observed temperature dependence of the spin gap provides strong evidence for ordering of Re orbitals at ~ 150 K, in accordance with an earlier proposal put forward by K. Oikawa *et al.* based on neutron diffraction [*J. Phys. Soc. Jpn.* **72**, 1411 (2003)] as well as recent theoretical work by Lee and Marianetti [*Phys. Rev. B* **97**, 045102 (2018)]. The presence of separate orbital and magnetic ordering in $\text{Ca}_2\text{FeReO}_6$ suggests weak coupling between spin and orbital degrees of freedom and hints at a subdominant role played by spin-orbit coupling in describing its magnetism. In addition, we observed only one well-defined magnon band near the magnetic zone boundary, which is incompatible with simple ferrimagnetic spin waves arising from Fe and Re local moments but suggests a strong damping of the Re magnon mode.

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I. INTRODUCTION

Magnetism in a 3d-5d ordered double perovskite (DP) $A_2MM'O_6$, where A is a cation and M and M' are 3d and 5d transition-metal ions, has been an area of intense research [1–18]. Formed by alternately arranged 3d M and 5d M' ions in a (nearly) cubic lattice [19], their magnetic properties may change dramatically depending on the identities of M and M' ions. When the M site is occupied by nonmagnetic ions, 5d M' ions form a geometrically frustrated fcc lattice, which is shown to exhibit a variety of magnetic ground states ranging from magnetic and/or orbital order [1–5,20–22] to spin glasses [6,7] to exotic spin liquid phases [8,9]. With magnetic M -site ions, one expects dominant superexchange interaction between M and M' magnetic moments and a simple antiparallel arrangement between them. However, this simple picture is complicated by the presence of strong spin-orbit coupling (SOC) on 5d ions, which tend to lock their spin and orbital angular momenta into the so-called J_{eff} moments. Unlike isotropic Heisenberg interactions between spin-only moments, interactions between J_{eff} moments [20–22] and their interactions with spin-only 3d moments [23], both present in 3d-5d DPs, can be anisotropic and strongly bond

dependent. Competition between 5d-5d and 3d-5d interactions is behind the highly nontrivial magnetic order observed in a wide range of DPs [10–18].

An underlying assumption in the above discussion is the validity of the J_{eff} description of 5d ions. Since this is essentially an atomic description, where the physics is dominated by local energy scales such as SOC, crystal field, and electronic correlation, one expects it to work well in strongly Mott insulating DPs. On the other hand, one expects this picture to break down in metallic DPs in which a large electronic bandwidth of 5d ions mixes different J_{eff} levels and reduces the effects of SOC. It is interesting to ask whether the spin-orbit-locked J_{eff} picture arising from large SOC is still valid close to a Mott instability, where both the correlated and itinerant natures of 5d electrons are important. Among 3d-5d DPs, the $A_2\text{FeReO}_6$ ($A = \text{Ba}, \text{Sr}, \text{Ca}$ with increasing lattice distortion) series provides examples that are likely to be close to a Mott instability. This is evidenced by a large change in transport properties across the series: cubic $\text{Ba}_2\text{FeReO}_6$ and tetragonal $\text{Sr}_2\text{FeReO}_6$ are metallic/half metallic, while $\text{Ca}_2\text{FeReO}_6$ is insulating with a significant monoclinic lattice distortion [24]. Among the three DPs in the $A_2\text{FeReO}_6$ series, $\text{Ca}_2\text{FeReO}_6$ undergoes a thermally driven insulator to metal transition [25] at ~ 150 K, which hints at its closest proximity to a Mott instability.

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Theoretically, electronic properties of $A_2\text{FeReO}_6$ were recently investigated by density functional theory (DFT)+ U calculations by Lee and Marianetti [26]. They showed that the Hubbard term on Re sites in $A_2\text{FeReO}_6$ (U_{Re}) is very close to the critical value for a Mott transition. In contrast to the above local picture where SOC plays an important role, they found that lattice distortion and Re electron correlation were the determining factors for electronic properties of $A_2\text{FeReO}_6$, while SOC was less important. In particular, tilting of ReO_6 octahedra and large U_{Re} enhance the tendency for Re orbital order and lead to the insulating ground state of $\text{Ca}_2\text{FeReO}_6$. On the other hand, they predicted orbital order is absent in less distorted $\text{Sr}_2\text{FeReO}_6$, which has a metallic ground state. Based on their calculation, such orbital order should also be absent in $\text{Ba}_2\text{FeReO}_6$, which is the least distorted member of $A_2\text{FeReO}_6$.

Structural evidence of orbital ordering in $\text{Ca}_2\text{FeReO}_6$ was reported in a neutron diffraction study by Oikawa *et al.* [18]. They observed a slight change in distortion of ReO_6 and FeO_6 octahedra without any change in lattice symmetry across the metal-insulator transition. Specifically, they found that the octahedra went from a compressed one along c at $T > 150$ K to an elongated one where the axis of elongation alternates between a and b for neighboring Re sites at $T < 150$ K. In addition, they also observed a reorientation of ordered moments from the c axis to the ab plane going from the high-temperature to low-temperature phase, which was argued to be a consequence of orbital ordering. Although structural distortion observed by Oikawa *et al.* [18] is suggestive of orbital ordering, it alone cannot unambiguously confirm the presence of orbital order in $\text{Ca}_2\text{FeReO}_6$ as lattice distortion has also been observed in $\text{Ba}_2\text{FeReO}_6$, in which the crystal goes from cubic to tetragonal below the magnetic ordering temperature [17], which, according to Lee and Marianetti [26], does not have orbital order.

Since magnetic interactions in Fe-Re double perovskites are strongly dependent on Re orbital states through SOC, another way to probe orbital ordering in these DPs is by measuring their magnetic excitations. Therefore, to examine orbital order in $\text{Ca}_2\text{FeReO}_6$ and gain a systematic understanding of magnetism in $A_2\text{FeReO}_6$, we studied magnetic excitations in $\text{Ca}_2\text{FeReO}_6$ using inelastic neutron scattering and compared the results with those for previously studied $\text{Ba}_2\text{FeReO}_6$ [27]. We found that spin excitation of $\text{Ca}_2\text{FeReO}_6$ is quite similar to that of $\text{Ba}_2\text{FeReO}_6$ in that a gapless magnon mode dominates the low-energy region, and the magnon bandwidth is ~ 50 meV. However, a large energy gap of ~ 10 meV opens up in the magnon spectrum for $T \lesssim 150$ K, which is well below the magnetic ordering temperature (~ 520 K [28]) but coincides with the proposed orbital ordering transition [25]. Opening of the magnon gap directly indicates an increase of low-symmetry magnetic interactions for $T \lesssim 150$ K and therefore provides strong evidence for orbital ordering. On the other hand, gapless magnetic excitations were observed in $\text{Ba}_2\text{FeReO}_6$ that persist down to ~ 30 K, indicating the absence of such an orbital ordering. We argue that separate magnetic and orbital ordering transitions in double perovskite $\text{Ca}_2\text{FeReO}_6$ as well as magnetic order without orbital order in $\text{Ba}_2\text{FeReO}_6$ suggest a separation between spin and orbital degrees of freedom in these double perovskites. This indicates

a subdominant role of SOC in describing the magnetism of $A_2\text{FeReO}_6$. In addition, we observed only one magnon band near the magnetic zone boundary. We showed that this is inconsistent with ferrimagnetic spin-wave dispersions consisting of localized Fe and Re spins and instead suggests the coexistence of damped and undamped magnon modes.

II. EXPERIMENTAL DETAILS

A polycrystalline sample of $\text{Ca}_2\text{FeReO}_6$ (8.9 g) was synthesized using standard solid-state methods, as reported elsewhere [24,26]. Magnetization measurements were carried out on a pelletized polycrystalline sample using a Quantum Design magnetic property measurement system (MPMS).

Time-of-flight inelastic neutron measurements were performed using the fine-resolution Fermi chopper spectrometer (SEQUOIA) at the Spallation Neutron Source at Oak Ridge National Laboratory [29,30]. Measurements were carried out using incident neutron energies of either 30 or 120 meV. The high-resolution Fermi chopper 2 rotating at frequencies of 360 and 600 Hz was used for $E_i = 30$ meV and $E_i = 120$ meV, respectively. Divergence of the incident neutron beam at the sample position due to the neutron guide is approximately 20 and 10 arcmin for $E_i = 30$ meV and $E_i = 120$ meV. A scattered neutron travels a distance of 5.5 m before reaching the detector array. An energy resolution of $\Delta E/E \sim 1.7\%$ was achieved for both incident energies at elastic energy. The sample was loaded into a flat aluminum container and mounted on a closed-cycle cryostat capable of reaching temperatures from 5 to 550 K. A series of “empty-can” data sets were collected under the same experimental conditions and used in background subtraction.

Neutron scattering measurements were also performed using the C5 spectrometer at the National Research Universal (NRU) reactor at Chalk River Laboratories on the same sample. These measurements were carried out with $E_i = 13.7$ meV using pyrolytic graphite (PG) as both a monochromator and analyzer, with a crystal mosaic of ~ 33 and 30 arcmin, respectively. Natural horizontal and vertical collimations of the beam from the reactor are ~ 33 and 72 arcmin. By using a collimation of none to 48 to 51 to 144 arcmin along the beam path, an energy and momentum resolution of ~ 1.2 meV and $\sim 0.04 \text{ \AA}^{-1}$ was achieved at the elastic line. A PG filter was used to suppress the contamination due to higher-order neutrons in the scattered beam.

III. RESULTS

The scattered neutron intensity is plotted as a function of energy transfer $\hbar\omega = E_i - E_f$ and momentum transfer $|\mathbf{Q}| = |\mathbf{k}_i - \mathbf{k}_f|$ in Figs. 1(a)–1(d) for various temperatures. Highly dispersive magnetic excitations extending up to ~ 50 meV can be clearly resolved in the low- $|\mathbf{Q}|$ region below 3 \AA^{-1} . Similar dispersive magnetic excitations were observed in $\text{Ba}_2\text{FeReO}_6$ and attributed to powder averaged spin wave modes within linear spin wave theory [27]. In addition to magnons, we also observed two modes at ~ 10 and ~ 20 meV which are indicated by black arrows in Fig. 1. They can be attributed to optical phonon modes as their intensities clearly increase with $|\mathbf{Q}|$. Here we focus on only magnetic excitations in the

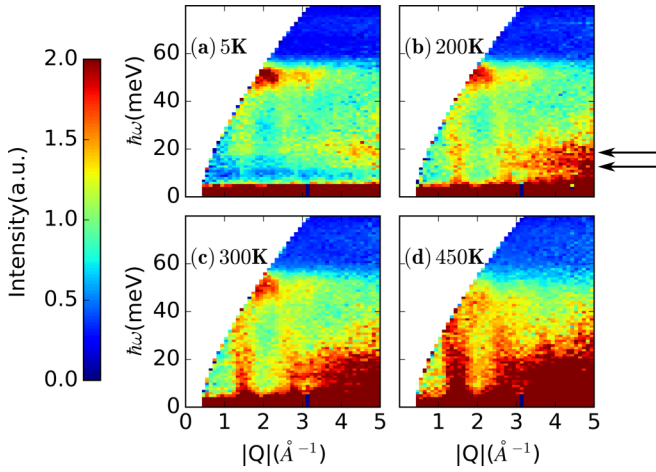


FIG. 1. Powder averaged neutron intensity plots measured with incident energy $E_i = 120$ meV at various temperatures: (a) 5, (b) 200, (c) 300, and (d) 450 K. The horizontal and vertical axes denote momentum $|Q|$ (\AA^{-1}) and energy transfers $\hbar\omega$ (meV). Two optical phonon modes discussed in the text are indicated by black arrows in (b). The aluminum sample container background has been subtracted from each scan, and an arbitrary intensity scale has been used where red (blue) denotes higher (lower) intensity.

small- $|Q|$ region. To compare scattering at different temperatures, inelastic neutron intensity is divided by the Bose factor defined as $[n(\omega, T) + 1]$ to obtain the local susceptibility $\chi''(|Q|, \omega)$. Here $n(\omega, T) = \frac{1}{\exp(\hbar\omega/k_B T) - 1}$. A large peak of magnon intensity at $\hbar\omega \approx 50$ meV is revealed by integrating $\chi''(|Q|, \omega)$ within $0.9 \text{ \AA}^{-1} < |Q| < 2.7 \text{ \AA}^{-1}$ as in Fig. 2(a), where the magnetic contribution dominates. This corresponds to a peak in the magnon density of states at the magnetic zone boundary energy that results from a Van Hove singularity at the top of the magnon band. This peak remains more or less temperature independent up to 300 K. A strong damping of the spin wave mode at $\hbar\omega \approx 50$ meV is observed at 450 K, which is clearly shown by a drastic drop in the peak intensity and slight softening in Fig 2(a). Since magnon modes are thermally populated when their energies are comparable to

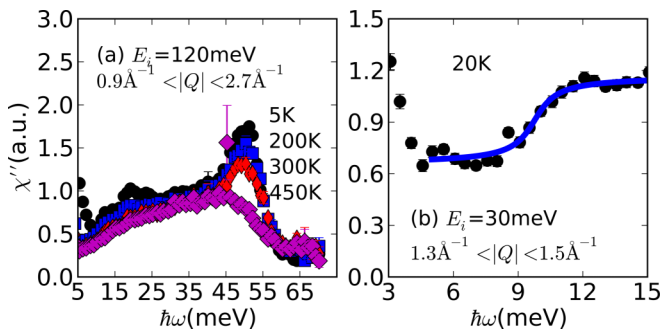


FIG. 2. Momentum-integrated local susceptibility χ'' (a) at 5, 200, 300, and 450 K with incident energy $E_i = 120$ meV and (b) at 20 K obtained with incident energy $E_i = 30$ meV [Fig. 3(a)]. The solid line is a fit to the phenomenological form described in the text. The Al sample container background has been subtracted, and the same arbitrary intensity scales as in Figs. 1 and 3 have been used for both (a) and (b).

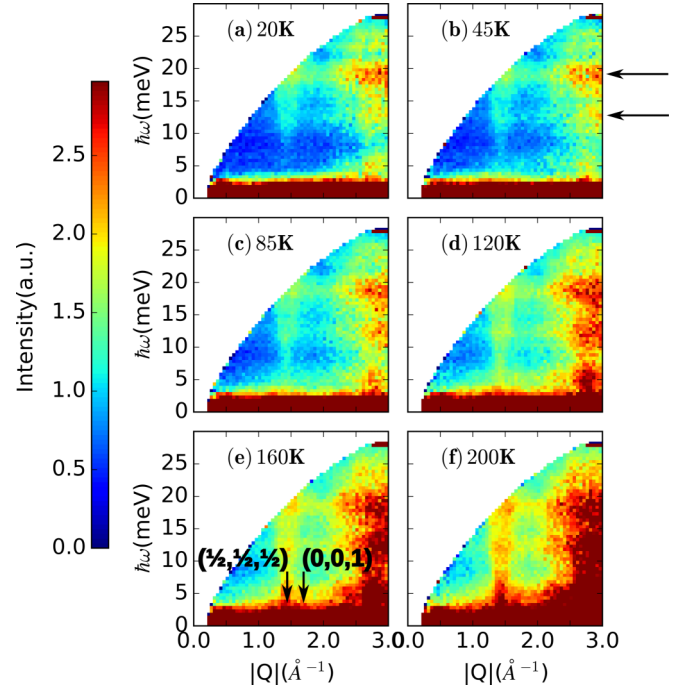


FIG. 3. Powder averaged neutron intensity plots with incident energy $E_i = 30$ meV at (a) 20, (b) 45, (c) 85, (d) 120, (e) 160, and (f) 200 K. This data are similar to those of Fig. 1 but were obtained with a higher-resolution setup. Two modes at ~ 10 and ~ 20 meV indicated by black arrows in (b) correspond to the optical phonon modes seen in high- E_i data in Fig. 1. Arrows in (e) denote positions for $\mathbf{Q} = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ and $\mathbf{Q} = (0, 0, 1)$ in pseudocubic notation. The Al sample container background has been subtracted from all plots.

thermal energy, zone boundary magnons ($\hbar\omega \sim 50$ meV) are expected to be strongly damped by magnon-magnon interactions at high temperature ($k_B T \sim 50$ meV or $T \sim 500$ K), in agreement with our observation.

Interestingly, compared to the spin excitation spectrum at 200 K, magnon intensity seems to be strongly suppressed for energy transfer $\hbar\omega \lesssim 10$ meV at 20 K. To study the temperature dependence of low-energy magnetic excitation in detail, we carried out high-resolution inelastic neutron scattering experiments with incident energy $E_i = 30$ meV. Figure 3 shows representative neutron scattering intensity plots between 20 and 200 K, obtained with $E_i = 30$ meV. With better momentum resolution, one can clearly see that spin wave intensity is strong near $|Q_1| \sim 1.4 \text{ \AA}^{-1}$, corresponding to the ordering wave vector at $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ in pseudocubic notation with $a \approx 3.8 \text{ \AA}$ (we used pseudocubic notation because monoclinic distortion from an ideal cubic unit cell in $\text{Ca}_2\text{FeReO}_6$ is too small to see with our experimental momentum resolution). On the other hand, $|Q_2| \sim 1.6 \text{ \AA}^{-1}$ corresponds to another Brillouin Zone center (0,0,1) where we observed negligible magnon intensity. Although both magnetic and structural peaks are allowed at each wave vector, giving rise to magnon and phonon contributions to the neutron intensity, the predominant magnetic contribution near \mathbf{Q}_1 is consistent with a stronger magnetic Bragg peak at \mathbf{Q}_1 . Due to a ferrimagnetic arrangement of Fe and Re moments, denoted by μ_{Fe} and μ_{Re} , respectively, the ratio between the

magnetic Bragg peak intensity at \mathbf{Q}_1 and \mathbf{Q}_2 is proportional to $\left(\frac{\mu_{\text{Fe}} + \mu_{\text{Re}}}{\mu_{\text{Fe}} - \mu_{\text{Re}}}\right)^2$, which indicates a negligible magnetic contribution to the Bragg intensity at $|\mathbf{Q}_2|$ compared to $|\mathbf{Q}_1|$ [27]. A better energy resolution also allows us to observe clear suppression of the magnon intensity below ~ 10 meV at $T = 20$ K, which shows the opening of a spin gap at low temperatures. On the other hand, gapless magnetic excitations are seen in Fig. 3(e) (160 K) and Fig. 3(f) (200 K), suggesting closure of the spin gap at high temperatures.

To track the detailed temperature dependence of the spin gap, we studied the temperature dependence of the magnetic inelastic intensity by making constant-energy cuts around 6 meV (integrating over an energy transfer $5 \text{ meV} < \hbar\omega < 7 \text{ meV}$) at various temperatures from $T = 20$ K to $T = 200$ K. This energy is well below the spin gap (see below) but still higher than the energy resolution. Neutron intensity at a given temperature T and energy transfer $\hbar\omega = 6$ meV is given by

$$I(T) = I_0 + I_{ph} + I_{\text{magn}}. \quad (1)$$

In Eq. (1), I_0 denotes the temperature-independent background, including the elastic tail of incoherent scattering as well as the instrumental background. I_{ph} describes phonon scattering in both the sample and sample container. Its temperature dependence is well described by the Bose factor as $I_{ph} = [n(T) + 1]\chi_0$, where χ_0 is the temperature-independent local susceptibility due to the phonon. Here we have dropped the energy dependence in $n(\omega, T)$ as $\hbar\omega$ was fixed at 6 meV for all temperatures. Last, I_{magn} is the magnetic inelastic intensity from the sample. To properly account for I_0 , we subtracted data at 20 K from all other temperatures. The resulting difference spectra $\Delta I(T) \equiv I(T) - I(20 \text{ K})$ are shown in Fig. 4(a). Since $n(\omega, T) \approx 0$ at $T = 20$ K for $\hbar\omega = 6$ meV, Eq. (1) implies $\Delta I(T) = n(T)\chi_0 + I_{\text{magn}}$. As shown in Fig. 4(a), ΔI increases gradually with temperature, consistent with phonon behavior for most $|\mathbf{Q}|$ (see also the Supplemental Material for quantitative analysis of the phonon background [31]). On the other hand, although the intensity near the strong magnetic Bragg peak $|\mathbf{Q}_1|$ follows that of the phonon background at 45 and 85 K, it increases much more rapidly at higher temperatures. Integrated intensity at $|\mathbf{Q}_1|$ is shown in the inset of Fig. 4(a). We also showed intensity at $|\mathbf{Q}_2|$ for comparison. Clearly, ΔI at $|\mathbf{Q}_2|$ follows the $n(T)$ dependence of the phonon background (blue solid line) for all temperatures. In contrast, ΔI at $|\mathbf{Q}_1|$ rises above the blue line for $T \gtrsim 100$ K, suggesting an increase in neutron intensity due to I_{magn} . To obtain I_{magn} at both $|\mathbf{Q}|$, a phonon background proportional to $n(T)$ was subtracted from ΔI at each $|\mathbf{Q}|$, which is shown in Fig. 4(b). I_{magn} near $|\mathbf{Q}_2|$ remains almost zero for all temperatures. On the other hand, I_{magn} near $|\mathbf{Q}_1|$ is zero for $T < 100$ K; it increases rapidly going from 100 to 150 K and saturates for $T > 150$ K. As discussed previously, intensity near $|\mathbf{Q}_1|$ ($|\mathbf{Q}_2|$) is dominated by the magnon (phonon) due to a stronger (weaker) magnetic Bragg peak. Different temperature dependences of I_{magn} near these two $|\mathbf{Q}|$ unambiguously show the filling of magnon intensity due to the closing of the spin gap.

To determine the gap size, the neutron intensity in Fig. 3(a) corrected by the Bose factor is integrated from 1.3 to 1.5 \AA^{-1}

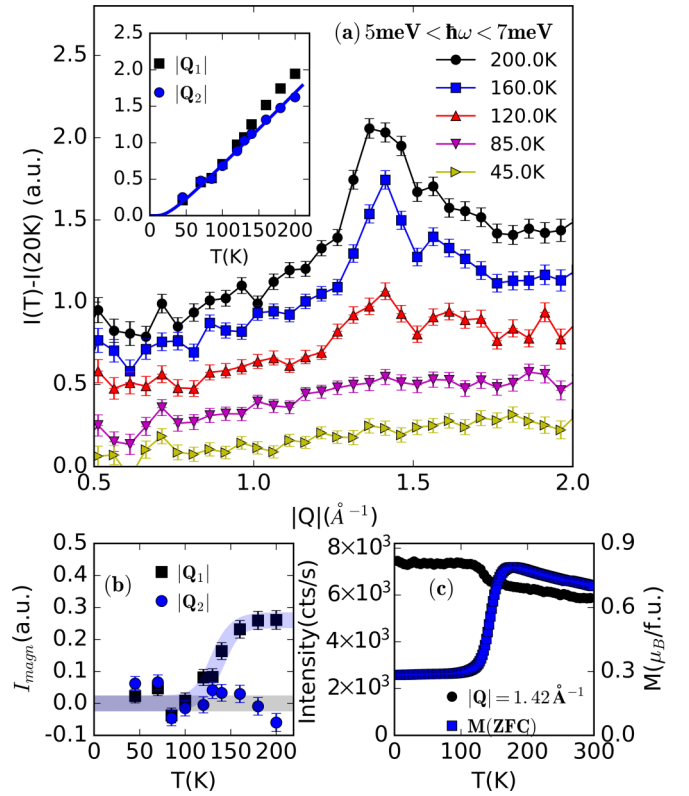


FIG. 4. (a) Constant-energy cuts below the gap obtained by integrating inelastic neutron intensity in Fig. 3 over energy transfers $5 \text{ meV} < \hbar\omega < 7 \text{ meV}$. The 20 K data have been subtracted from all plots. Inset: Intensity at $|\mathbf{Q}_1|$ and $|\mathbf{Q}_2|$ as a function of temperature, obtained by integrating constant-energy cuts in the main plot within $1.3 \text{ \AA}^{-1} < |\mathbf{Q}| < 1.5 \text{ \AA}^{-1}$ and $1.5 \text{ \AA}^{-1} < |\mathbf{Q}| < 1.7 \text{ \AA}^{-1}$. Blue solid line shows $n(T)$ for $\hbar\omega = 6$ meV. It has been scaled to match the data at $|\mathbf{Q}_2|$. (b) Temperature dependence of magnetic inelastic intensity I_{magn} at $|\mathbf{Q}_1|$ (black square) and $|\mathbf{Q}_2|$ (blue circle). I_{magn} is obtained by subtracting the phonon intensity given by $n(T)$ from integrated intensities in the inset of (a). (c) Temperature dependence of the magnetic Bragg peak intensity at $|\mathbf{Q}_1|$ and zero-field cooled (ZFC) magnetization of a $\text{Ca}_2\text{FeReO}_6$ pellet. Magnetization was obtained in the presence of an applied field of 0.2 T after cooling down to 2 K in zero field. Magnetic Bragg peak intensity was obtained at the C5 triple-axis spectrometer at NRU at fixed $|\mathbf{Q}| = 1.42 \text{ \AA}^{-1}$ and $\hbar\omega = 0$ meV on the same powder sample used for time-of-flight measurements.

around $|\mathbf{Q}_1|$ and plotted as a function of energy transfer as in Fig. 2(b). The resulting local susceptibility χ'' is suppressed below $\hbar\omega \sim 10$ meV, indicating the presence of a spin gap. Data from 5 to 15 meV were fit to the step function $A \tan^{-1}(\frac{\omega - \Delta}{\Gamma}) + B$, where A , Δ , and Γ denote the height, center, and width of the step function and B denotes the background. The gap size, defined as the center of the step function Δ , is determined to be $9.8(5)$ meV.

A drastic change in low-energy magnetic dynamics is also reflected in the temperature dependence of the magnetic Bragg peak intensity, which is proportional to the square of static moment size. As shown in Fig. 4(c), the magnetic Bragg peak intensity at $|\mathbf{Q}_1|$ remains constant for $T < 100$ K. It drops rapidly as temperature increases from 100 to 150 K and

continues to decrease gradually for $T > 150$ K. The gradual decrease in magnetic Bragg intensity for $T > 150$ K is consistent with the observed spin gap closing since increases in spin fluctuation with thermal population of low-energy magnons would reduce the static moments with increasing temperature. On the other hand, magnetic Bragg intensity remains unchanged for $T < 100$ K since low-energy spin fluctuations are preempted by the presence of a large spin gap. The abrupt $\sim 15\%$ drop in the $|\mathbf{Q}_1|$ Bragg peak intensity from 100 to 150 K shown in Fig. 4(c) was also observed in the neutron diffraction study by Oikawa *et al.* [18] and was attributed to reorientation of magnetic moments due to orbital ordering from Rietveld analysis.

Since the isotropic Heisenberg Hamiltonian is rotationally invariant, the magnon spectrum should be gapless by the Goldstone theorem. The presence of the magnon gap at low temperature thus requires single-ion anisotropy or anisotropic exchange terms that break the full rotational symmetry of the magnetic Hamiltonian. Gapless spectra observed in the high-temperature phase of $\text{Ca}_2\text{FeReO}_6$ as well as in $\text{Ba}_2\text{FeReO}_6$ suggest the removal of the anisotropy terms. This picture is consistent with bulk magnetization data shown in Fig. 4(c). For $T < 100$ K, ordered moments are confined to crystallographic directions favored by the anisotropy terms, which are randomly oriented in a powder sample and lead to small overall magnetization when field is not too large. For $T > 150$ K, the absence of anisotropy means that ordered moments can be freely aligned by an external field, leading to the observed large increase in magnetization. A significant drop in coercive field was also observed going from 100 to 150 K, consistent with a decrease in magnetic anisotropy [32].

IV. DISCUSSION

Our neutron scattering results show that $\text{Ca}_2\text{FeReO}_6$ exhibits a well-defined spin wave excitation in the magnetically ordered phase. The spin excitation is gapless for $T \gtrsim 150$ K and becomes gapped (with a gap size of ~ 10 meV) below ~ 150 K, coinciding with the reported metal-insulator transition [25] and onset of structural distortion [18]. The structural distortion has been interpreted as a consequence of Re orbital ordering both by considering the effects of ReO_6 octahedra distortion on local crystal field levels [18] and by a DFT calculation [26].

Since distortion of the orbital electron density is more pronounced in the presence of strong orbital ordering, one expects larger low-symmetry magnetic interactions in the orbitally ordered phase due to spin orbit coupling. This is entirely consistent with the gap opening shown by our neutron scattering results at low temperatures. Therefore, our results provide compelling evidence for orbital order in $\text{Ca}_2\text{FeReO}_6$ for $T \lesssim 150$ K. Quantitatively, inclusion of SOC in DFT calculations in the orbitally ordered phase give rise to easy-axis anisotropy along b with a magnetic anisotropy energy per Re atom of ~ 6 meV [26], in rough agreement with the gap size (~ 10 meV) observed in our data. Slight structural distortion was also observed in $\text{Ba}_2\text{FeReO}_6$ below the magnetic transition temperature [17]. Unlike $\text{Ca}_2\text{FeReO}_6$, its magnon spectrum remains gapless throughout the magnetically ordered phase [27]. A comparison between $\text{Ca}_2\text{FeReO}_6$ and

$\text{Ba}_2\text{FeReO}_6$ therefore indicates that no actual orbital order occurs in $\text{Ba}_2\text{FeReO}_6$. The stronger tendency of orbital order in $\text{Ca}_2\text{FeReO}_6$ was attributed to a larger tilt of ReO_6 octahedra by Lee and Marianetti [26].

Separate magnetic and orbital ordering transitions in $\text{Ca}_2\text{FeReO}_6$ as well as magnetic order without orbital order in $\text{Ba}_2\text{FeReO}_6$ indicate weak coupling between spin and orbital degrees of freedom in A_2FeReO_6 . This is somewhat surprising given the large SOC of Re ions. In a recently popular atomic picture in which local physics is determined by SOC and crystal field, Re spin and orbital angular momenta are locked into $J_{\text{eff}} = 2$ local moments that interact through highly anisotropic interactions, as shown theoretically by Chen and Balents [22].

Although experimental signatures for anisotropic interactions are largely lacking in rhenates, gapped magnon spectra consistent with anisotropic interactions between J_{eff} moments have been observed in many osmate and iridate compounds with chain [33–35], layered [36,37], perovskite [38], and double-perovskite structures [1,39–42]. Among the double perovskites studied, $\text{Sr}_2\text{ScOsO}_6$ (with magnon gap $\Delta = 12$ meV) [40], $\text{Sr}_2\text{MgOsO}_6$ ($\Delta = 7$ meV) [41], $\text{Ba}_2\text{ZnOsO}_6$ ($\Delta = 7$ meV), and $\text{Ba}_2\text{MgOsO}_6$ ($\Delta = 12$ meV) [42] contain an Os^{6+} ion with the same electronic configuration as Re^{5+} and hence directly indicate the importance of anisotropic interactions between $5d^2$ ions.

Gapless magnetic excitations observed in magnetically ordered phases therefore suggest a subdominant role of SOC in A_2FeReO_6 . This also explains the separation of spin and orbital degrees of freedom in A_2FeReO_6 . Theoretically, Lee and Marianetti [26] showed that the electronic properties of A_2FeReO_6 were determined mainly by electronic correlation and lattice distortion and were not qualitatively changed by SOC. This is consistent with the discussions based on our experimental observation. Small effects of SOC in $\text{Ba}_2\text{FeReO}_6$ have been inferred from a branching ratio of ~ 2 determined by x-ray absorption spectroscopy [43], which is similar to the statistical value expected in the absence of SOC [44]. Qualitatively, small effects of SOC in A_2FeReO_6 might be explained by a large Re bandwidth due to strong hybridization with surrounding Fe ions. A large electronic bandwidth mixes different J_{eff} levels and weakens the effects of SOC. The breakdown of the J_{eff} picture is also supported by the resonant inelastic x-ray scattering measurement on A_2FeReO_6 reporting highly damped intra- t_{2g} excitations [45].

We note that recent inelastic neutron scattering on another $3d$ - $5d$ DP with a magnetic $3d$ ion, $\text{Sr}_2\text{FeOsO}_6$ [46], also showed a gap opening below a secondary phase transition, somewhat similar to $\text{Ca}_2\text{FeReO}_6$. However, the gap opening in $\text{Sr}_2\text{FeOsO}_6$ is accompanied by a magnetic structure change [13], which is different from $\text{Ca}_2\text{FeReO}_6$, where magnetic order remains unchanged. In addition, OsO_6 octahedra actually become more symmetrical in the low-temperature phase of $\text{Sr}_2\text{FeOsO}_6$ [47]. Therefore, the origin of the gap opening in $\text{Sr}_2\text{FeOsO}_6$ is different from that in $\text{Ca}_2\text{FeReO}_6$.

So far we have focused on the low-energy part of magnetic excitations in $\text{Ca}_2\text{FeReO}_6$. We now move on to discuss its high-energy part. One puzzling feature of high-energy spin excitations is the observation of only one strong magnon band at $\hbar\omega \approx 50$ meV, as shown in Fig. 1(a). Since $\text{Ca}_2\text{FeReO}_6$

consists of Fe and Re moments of different sizes, one expects two magnon modes and hence two strong bands of inelastic intensity coming from zone boundary magnons within ferrimagnetic spin wave theory. One possibility is an accidental merging of Fe and Re magnon bands at the zone boundary. In the Appendix, we show that this is unlikely because we did not observe splitting of the two bands by the anisotropy terms responsible for opening a spin gap at low temperatures. Another possibility is that the observed spin wave comes from only Fe local moments, while the dynamics of Re electrons are much faster and can be integrated out. This $3d$ spin-only model was proposed for $\text{Sr}_2\text{FeMoO}_6$ and $\text{Sr}_2\text{CrOsO}_6$ [48,49]. Since Fe magnetic moments are ferromagnetically ordered, we expect the spin wave intensity to be strong at both “antiferromagnetic” $\mathbf{Q} (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ and “ferromagnetic” $\mathbf{Q} (0, 0, 1)$ in a Fe spin-only model. However, we observed strong magnetic inelastic intensity only at $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$, as shown in Fig. 3. Therefore, we conclude that Re magnetic moments must contribute to spin dynamics in $\text{Ca}_2\text{FeReO}_6$. The most plausible explanation for the observation of only one magnon band is therefore selective damping of the Re magnon. This might be due to the strong charge fluctuation on the Re sites, which is expected from the close proximity of Re electrons to a Mott instability. On the other hand, localized Fe moments give rise to a well-defined spin wave mode seen at ~ 50 meV.

V. CONCLUSIONS

In summary, we have carried out inelastic neutron scattering studies on $\text{Ca}_2\text{FeReO}_6$. We found well-defined spin wave excitations that are gapless for $T \gtrsim 150$ K but become gapped at ~ 150 K. This provides strong dynamical evidence for orbital ordering below ~ 150 K in $\text{Ca}_2\text{FeReO}_6$ proposed by a previous structural study [18] and recent DFT+ U calculations [26]. On the other hand, no spin gap was found in $\text{Ba}_2\text{FeReO}_6$ [27], which indicates the absence of such orbital ordering, consistent with theoretical predictions. We argued that unlike other $5d$ materials in which spin-orbit coupling is essential for describing the magnetic dynamics, SOC plays a subdominant role in describing the magnetism of A_2FeReO_6 .

Moreover, we found only one zone boundary magnon band in $\text{Ca}_2\text{FeReO}_6$, which strongly contradicts the simple ferrimagnetic spin wave picture. This points to the coexistence of undamped Fe and strongly damped Re magnon modes. To test this possibility, future polarized neutron or resonant inelastic x-ray scattering on single crystals of $\text{Ca}_2\text{FeReO}_6$ that can resolve Fe and Re magnon modes is desirable.

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APPENDIX: SPIN WAVE ANALYSIS

In this appendix, we explore the potential merging of Fe and Re magnon modes in a local moment model. The Fe/Re local moment model used here is similar to that considered by Plumb *et al.* [27]. In addition to the nearest-neighbor Fe-Re coupling \mathcal{J}_0 , we also included next-nearest-neighbor Re-Re

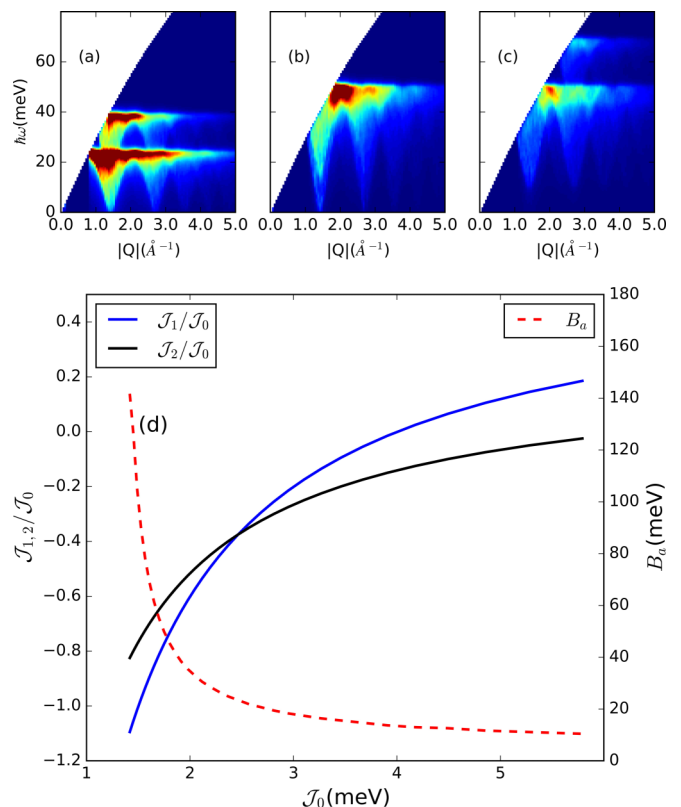


FIG. 5. Simulated powder averaged spin wave spectra using $\mathcal{F} = 2.1$ and $\mathcal{R} = 1.3$ for (a) $\mathcal{J}_0 = 3.1$ meV, $\mathcal{J}_1 = \mathcal{J}_2 = B_a = 0$, (b) $\mathcal{J}_0 = 2.9$ meV, $\mathcal{J}_1 = -0.7$ meV, $\mathcal{J}_2 = -0.8$ meV, $B_a = 0$, and (c) $\mathcal{J}_0 = 2.9$ meV, $\mathcal{J}_1 = -0.7$ meV, $\mathcal{J}_2 = -0.8$ meV, $B_a = 18.6$ meV. Calculation of powder averaged spectra is done using the SPINW package [50]. All spectra have been corrected for magnetic form factors and instrumental resolutions. (d) Left axis: $\{\mathcal{J}_0, \mathcal{J}_1, \mathcal{J}_2\}$ parameters constrained by setting zone boundary energies of both modes in the local moment model to 50 meV. The horizontal axis denotes the absolute magnitude of the nearest Fe-Re interaction \mathcal{J}_0 . The vertical axis denotes the magnitude of next-nearest-neighbor Re-Re and Fe-Fe interactions relative to the nearest-neighbor interaction, $\mathcal{J}_1/\mathcal{J}_0$ and $\mathcal{J}_2/\mathcal{J}_0$. Right axis: The effective anisotropy field B_a required to produce a gap of 10 meV for each set of $\{\mathcal{J}_0, \mathcal{J}_1, \mathcal{J}_2\}$.

and Fe-Fe couplings, \mathcal{J}_1 and \mathcal{J}_2 ,

$$\begin{aligned} \mathcal{H} = & \mathcal{J}_0 \sum_{\langle i,j \rangle} \vec{\mathcal{F}}_i \cdot \vec{\mathcal{R}}_j + \mathcal{J}_1 \sum_{\langle i,i' \rangle} \vec{\mathcal{R}}_i \cdot \vec{\mathcal{R}}_{i'} \\ & + \mathcal{J}_2 \sum_{\langle j,j' \rangle} \vec{\mathcal{F}}_j \cdot \vec{\mathcal{F}}_{j'} - B_a \sum_i \mathcal{R}_{z,i}, \end{aligned} \quad (\text{A1})$$

where $\vec{\mathcal{R}}_i$ and $\vec{\mathcal{F}}_j$ denote effective Re and Fe local moments, respectively. In A_2FeReO_6 , long-range Re-Re and Fe-Fe magnetic interactions are expected to be significant due to large electronic itinerancy at the proximity of a metal-insulator transition. An anisotropy term of the form $B_a \mathcal{R}_z$ has been added to account for the spin gap observed at low temperatures. It is equivalent to Ising anisotropy of the form $\mathcal{J}_z \mathcal{R}_{z,i} \mathcal{R}_{z,i'}$ and single-ion anisotropy $D\mathcal{R}_z^2$ within linear spin wave theory. Since terms like these come from strong spin-orbit coupling of Re, it is not included for the Fe moment, which is orbitally inactive with $S = \frac{5}{2}$. Energies of the two magnon modes are [51]

$$2\hbar\omega_{\pm}(\mathbf{Q}) = 2\Omega(\mathbf{Q}) \pm [B_a + b_1(\mathbf{Q}) - b_2(\mathbf{Q})],$$

where we defined the following terms:

$$b_1(\mathbf{Q}) = \mathcal{F}\mathcal{J}_0(\mathbf{0}) - \mathcal{R}[\mathcal{J}_1(\mathbf{0}) - \mathcal{J}_1(\mathbf{Q})],$$

$$b_2(\mathbf{Q}) = \mathcal{R}\mathcal{J}_0(\mathbf{0}) - \mathcal{F}[\mathcal{J}_2(\mathbf{0}) - \mathcal{J}_2(\mathbf{Q})],$$

$$2\Omega(\mathbf{Q}) = \{[B_a + b_1(\mathbf{Q}) + b_2(\mathbf{Q})]^2 - \mathcal{R}\mathcal{F}[2\mathcal{J}_0(\mathbf{Q})^2]\}^{\frac{1}{2}}.$$

Here we define $\mathcal{J}_{\alpha=0,1,2}(\mathbf{Q}) = \mathcal{J}_{\alpha} \sum_{\delta} \exp(i\delta \cdot \mathbf{Q})$, where δ denotes all neighboring sites coupled to the i th site by interaction \mathcal{J}_{α} .

First, we set $B_a = 0$, which corresponds to the high-temperature phase of $\text{Ca}_2\text{FeReO}_6$; two well-separated

magnon modes are predicted by linear spin wave theory with only nearest-neighbor interactions. This was demonstrated by Plumb *et al.* [27]. The calculated spin wave spectrum from Ref. [27] using $\mathcal{F} = 2.1$, $\mathcal{R} = 1.3$, and $\mathcal{J}_0 = 3.1$ meV is reproduced in Fig. 5(a).

The lower magnon branch can be moved up and made to coincide with the upper branch by turning on next-nearest-neighbor interactions. The observed magnon spectrum in $\text{Ca}_2\text{FeReO}_6$ can be captured qualitatively by setting zone boundary energies of both branches to 50 meV, which generates a range of allowed $\{\mathcal{J}_0, \mathcal{J}_1, \mathcal{J}_2\}$ depending only on the value of \mathcal{J}_0 , as shown in Fig. 5(d). The calculated spectrum using one set of the allowed parameters $\mathcal{J}_0 = 2.9$ meV, $\mathcal{J}_1 = -0.7$ meV, $\mathcal{J}_2 = -0.8$ meV is shown in Fig. 5(b). For comparison, we used the same values of \mathcal{F} and \mathcal{R} as in Plumb *et al.* [27].

Turning to the low-temperature data, we observed the spin gap to be 10 meV, which sets a constraint on B_a . As shown in Fig. 5(d), a large $B_a > 10$ meV is required to reproduce the observed spin gap for the entire range of interactions considered. Since degeneracy at the zone boundary is accidental, introducing a large anisotropy term splits the two zone boundary modes by the amount $\hbar\omega_+ - \hbar\omega_- = B_a$. This is explicitly shown in Fig. 5(c) for the interaction parameters used in Fig. 5(b). Such splitting is not observed in our data at low temperatures, which points to the inadequacy of the above spin wave analysis.

Another way to merge Fe and Re magnon modes in a local moment model is to use the same magnetic moment sizes for both Re and Fe. Like for the above discussions, we expect degeneracy of the two modes to be broken by anisotropy terms included only for Re sites at low temperatures. Moreover, identical magnetic moment sizes are ruled out by powder neutron diffraction [18], which refined Fe and Re moments to be $\sim 4\mu_B$ and $\sim 1\mu_B$ respectively.

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